

Exercises Section 1.4 [page 39]

**44.** The article “Oxygen Consumption During Fire Suppression: Error of Heart Rate Estimation” (*Ergonomics*, 1991: 1469-1474) reported the following data on oxygen consumption (mL/kg/min) for a sample of ten firefighters performing a fire-suppression simulation:

29.5 49.3 30.6 28.2 28.0 26.3 33.9 29.4 23.5 31.6

Compute the following:

- a. The sample range
- b. The sample variance  $s^2$  from the definition (i.e., by first computing deviations, then squaring them, etc.)
- c. The sample standard deviation
- d.  $s^2$  using the shortcut method

**45.** The value of Young's modulus (GPa) was determined for cast plates consisting of certain intermetallic substrates, resulting in the following sample observations (“Strength and Modulus of a Molybdenum-Coated Ti-25Al-10Nb-3U-1Mo Intermetallic,” *J. of Materials Engr. and Performance*, 1197: 46-50):

116.4 115.9 114.6 115.2 115.8

**a.** Calculate  $\bar{x}$  and the deviations from the mean.

**b.** Use the deviations calculated in part a to obtain the sample variance and the sample standard deviation.

**c.** Calculate  $s^2$  by using the computational formula for the numerator  $S_{xx}$ .

**d.** Subtract 100 from each observation to obtain a sample of transformed values. Now calculate the sample variance of these transformed values, and compare it to  $s^2$  for the original data.

**46.** The accompanying observations on stabilized viscosity (cP) for specimens of a certain grade of asphalt with 18% rubber added are from the article “Viscosity Characteristics of Rubber-Modified Asphalts” (*J. of Materials in Civil Engr.*, 1996: 153-156):

2781 2900 3013 2856 2888

**a.** What are the values of the sample mean and sample median?

**b.** Calculate the sample variance using the computational formula. [*Hint* First subtract a convenient number from each observation.]

**47.** Calculate and interpret the values of the sample median, sample mean, and sample standard deviation for the following observations on fracture strength (MPa, read from a graph in “Heat-Resistant Active Brazing of Silicon Nitride: Mechanical Evaluation of Braze Joints,” *Welding J.*, August, 1997):

87 93 96 98 105 114 128 131 142 168

**49.** A study of the relationship between age and various visual functions (such as acuity and depth perception) reported the following observations on area of scleral lamina ( $\text{mm}^2$ ) from human optic nerve heads (“Morphometry of Nerve Fiber Bundle Pores in the Optic Nerve Head of the Human,” *Experimental Eye Research*, 1988: 559-568):

2.75 2.62 2.74 3.85 2.34 2.74 3.93 4.21 3.88  
4.33 3.46 4.52 2.43 3.65 2.78 3.56 3.01

**a.** Calculate  $\sum x_i$  and  $\sum x_i^2$ .

**b.** Use the values calculated in part a to compute the sample variance  $s^2$  and then the sample standard deviation  $s$ .

**51.** The article “A Thin-Film Oxygen Uptake Test for the Evaluation of Automatic Crankcase Lubricants” (*Lubric. Engr.*, 1984: 75-83) reported the following data on oxidation-induction time (min) for various commercial oils:

87 103 130 160 180 195 132 145 211 105 145  
153 152 138 87 99 93 119 129

**a.** Calculate the sample variance and standard deviation.

**b.** If the observations were reexpressed in hours, what would be the resulting values of the sample variance and sample standard deviation? Answer without actually performing the reexpression.